

$$h(x) = \int_{-5}^x f(t) dt = F(x) - F(-5)$$

$$g(x) = \int_0^x f(t) dt = F(x) - F(0) \quad \int f(x) dx = F(x) + C$$

$$k(x) = \int_1^x f(t) dt = F(x) - F(1)$$

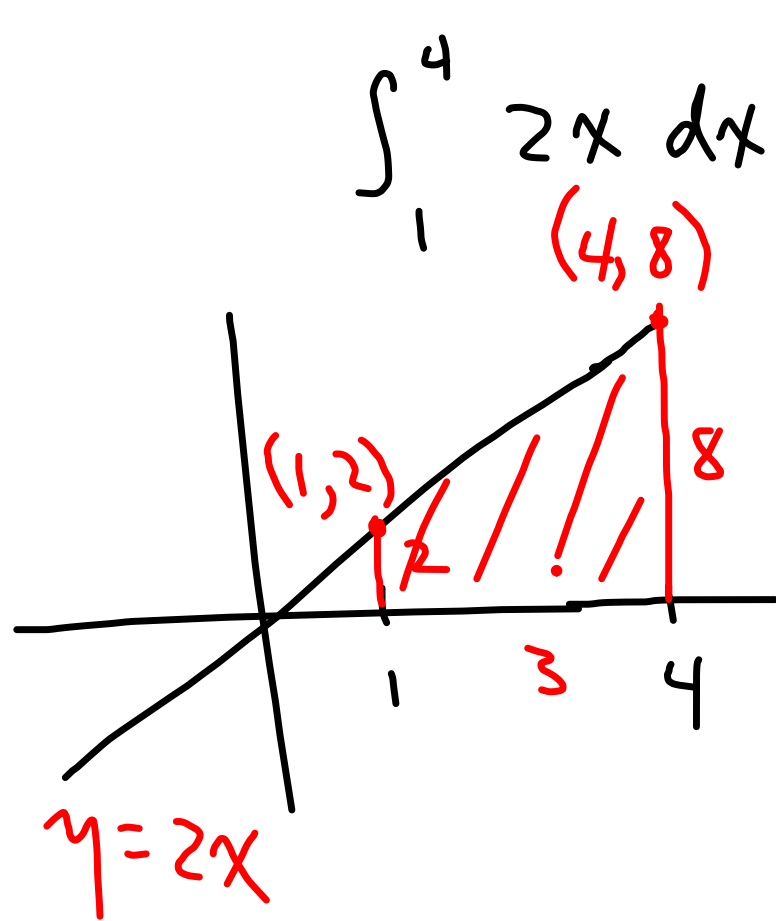
Let  $F(x)$  be an antiderivative  
of  $f(x)$  ( $F'(x) = f(x)$ )

$$\int_a^b f(x) dx = F(b) - F(a)$$

$$\frac{d}{dx} \int_a^x f(t) dt = \frac{d}{dx} [F(x) - F(a)] = f(x)$$

$F(x)$  is an antiderivative of  $f(x)$

$F'(x) = f(x)$	$F(x)$	$f(x)$
	$\sin x$	$\cos x$
	$\tan x$	$\sec^2 x$
	$\cot x$	$-\csc^2 x$
	$\csc x$	$-\csc x \cot x$
	$\ln x$	$\frac{1}{x}$
	$\log_a x$	$\frac{1}{x \ln a}$ or $\frac{1}{x} \cdot \frac{1}{\ln a}$
	$e^x$	$e^x$
	$a^x$	$a^x \ln a$



$$\int_1^4 2x \, dx = x^2 \Big|_1^4$$
$$= 16 - 1$$
$$= 15$$

$$\frac{d}{dx} \int_5^x \cos \sqrt{2t+1} dt = \cos \sqrt{2x+1}$$

$$\frac{d}{dx} \int_3^x \cos \sqrt{2t+1} dt = \cos \sqrt{2x+1}$$

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$$\frac{d}{dq} \int_q^3 2t dt = - \frac{d}{dq} \int_3^q 2t dt$$
$$= -2q$$

$$\frac{d}{dq} \left[ \int_q^3 f(t) dt \right] = \frac{d}{dq} \left[ F(3) - F(q) \right]$$
$$= -f(q)$$
$$-2q$$

$$\begin{aligned}\frac{d}{dx} \int_0^{x^2} \cos t \, dt &= \cos u \cdot 2x \\ &= \cos x^2 \cdot 2x \\ &= 2x \cos x^2\end{aligned}$$

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

$$y = \int_0^{x^2} \cos t \, dt \quad u = x^2$$

$$\frac{d}{du} \int_0^u \cos t \, dt = \cos u$$

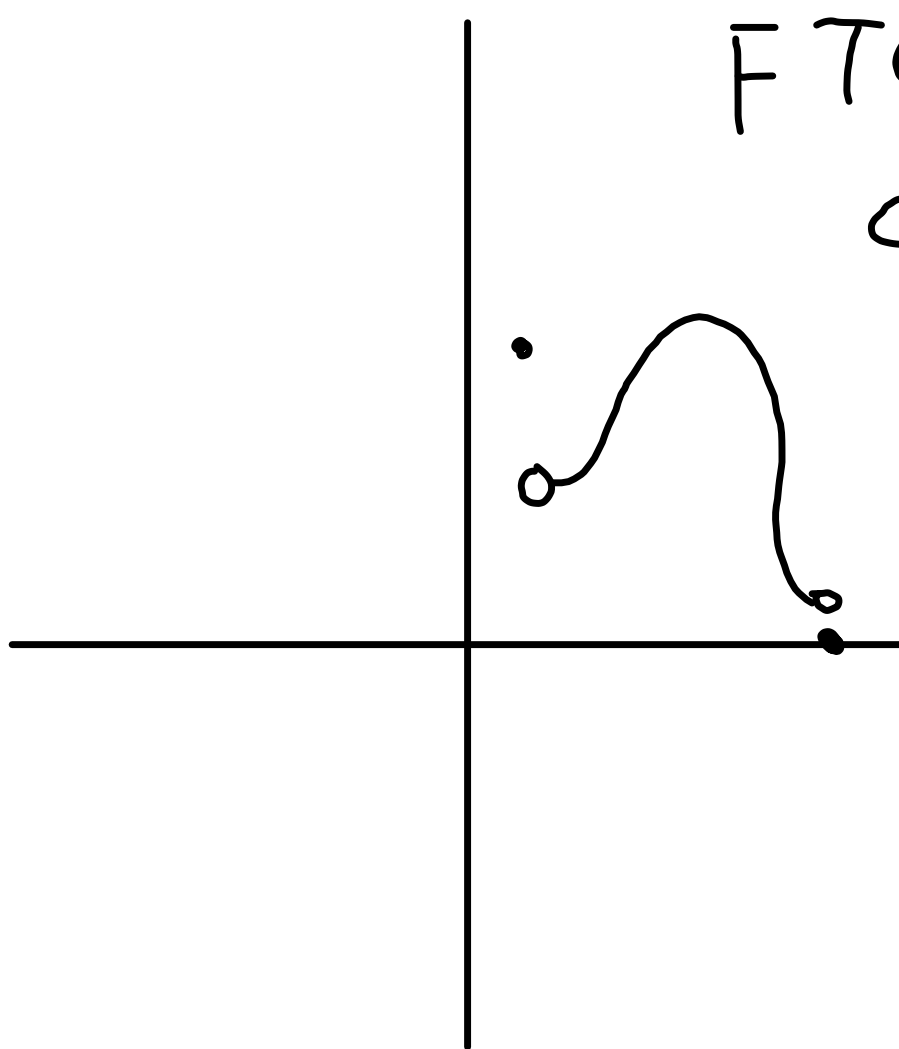
$$\frac{du}{dx} = 2x$$

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$$\frac{d}{dx} \int_0^{\cos x} \sqrt{t^2 - 7} \, dt = \quad u = \cos x$$

$$\frac{du}{dx} = -\sin x$$

$$\begin{aligned}\frac{d}{dx} \left( \int_0^u \sqrt{t^2 - 7} \, dt \right) &= \sqrt{u^2 - 7} \frac{du}{dx} \\ &= \sqrt{\cos^2 x - 7} \cdot (-\sin x) \\ &= -\sin x \sqrt{\cos^2 x - 7}\end{aligned}$$



FTC requires  
continuity on  
the closed  
interval  
defined by  
the bounds of  
integration

