

$$\frac{1}{3} \int 3x^2 \cos(x^3 - 3) dx \quad \begin{array}{l} \text{Let } u = x^3 - 3 \\ du = 3x^2 \cdot dx \end{array}$$

$$\frac{1}{3} \int \cos u \, du$$

$$\frac{1}{3} \sin u + C$$

$$\frac{1}{3} \sin(x^3 - 3) + C$$

$$\int_0^{\frac{\pi}{4}} \tan x \sec^2 x \, dx$$

$$\int_0^1 u \, du$$

$$\frac{u^2}{2} \Big|_0^1 = \frac{1}{2}$$

$$\int u \, du$$

$$\frac{u^2}{2} + C$$

$$\frac{\tan^2 x}{2} + C \Big|_0^{\frac{\pi}{4}}$$

$$\frac{1}{2} + C - (0 + C)$$

$$\frac{1}{2}$$

$$\text{Let } u = \tan x$$

$$du = \sec^2 x \, dx$$

$$u = \tan 0$$

$$u = 0$$

$$u = \tan \frac{\pi}{4}$$

$$u = 1$$

$$\frac{dy}{dx} = (y+5)(x+2)$$

$$\int \frac{1}{y+5} \frac{dy}{dx} dx = \int x+2 dx$$

$$\int \frac{1}{y+5} dy = \int x+2 dx$$

$$\begin{cases} \log_a b = k \\ a^k = b \end{cases}$$

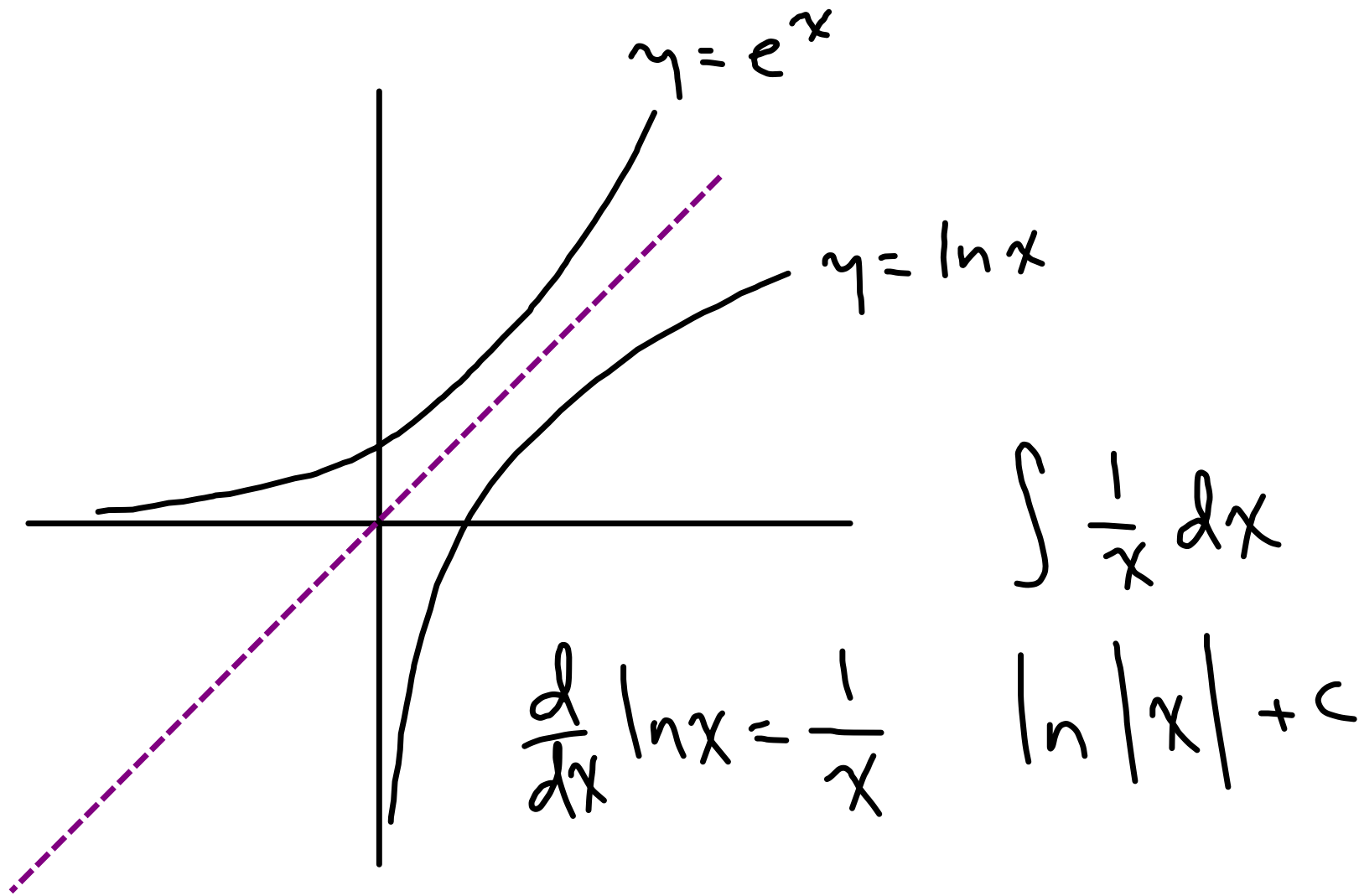
$$\ln |y+5| = \frac{x^2}{2} + 2x + C$$

$$|y+5| = e^{\frac{x^2}{2} + 2x + C}$$

$$\begin{aligned} a^m a^n \\ a^{m+n} \end{aligned}$$

$$y = e^{\frac{x^2}{2} + 2x + C} - 5$$

$$y = e^C \cdot e^{\frac{x^2}{2} + 2x} - 5$$



$$\frac{dy}{dx} = -2xy^2 \quad y(1) = .25$$

$$\int \frac{1}{y^2} dy = \int 2x dx$$

$$-y^{-1} + C_1 = -x^2 + C_2$$

$$y^{-1} = x^2 + C$$

$$\frac{1}{y} = x^2 + C$$

$$y = \frac{1}{x^2 + C}$$

$$.25 = \frac{1}{1 + C}$$

$$3 = C$$

The particular solution

$$y = \frac{1}{x^2 + 3}$$

General solution